This course satisfies the University of Texas at Arlington core curriculum requirement in mathematics.

**Description of Course Content:** This course is designed to prepare future elementary school teachers *mathematically* to teach math (as opposed to *pedagogically*, which is the goal of ECED/BEEP 4311 and EDML 4372). It does this in two main ways: by teaching math which is relevant (not identical) to the math they will be teaching, and by modeling a math classroom through problem-solving activities, cooperative groups, and holding students responsible for deciding (reasoning) what is correct. Basics of geometry, constructions, polygons, tessellations, polyhedra, symmetry, rigid motion, and measurement are the topics that will be studied.

**This course will address three objectives:**
- **Critical Thinking Skills** - to include creative thinking, innovation, inquiry, and analysis, evaluation and synthesis of information.
- **Communication Skills** - to include effective development, interpretation and expression of ideas through written, oral and visual communication.
- **Empirical and Quantitative Skills** - to include the manipulation and analysis of numerical data or observable facts resulting in informed conclusions.

**Syllabus:** An approximate schedule with topics is given below.

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<th>Unit Topic</th>
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<td>4 Tessellations</td>
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<td>Midterm</td>
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<td>Regular Polyhedra&lt;br&gt;Nonregular Polyhedra&lt;br&gt;Platonic Solids&lt;br&gt;Euler's Formula&lt;br&gt;Extending Polygons</td>
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<tr>
<td>5 Polyhedra</td>
<td>7</td>
<td>Symmetry of Planar Objects&lt;br&gt;Symmetry of 4D Objects&lt;br&gt;Extending Euler&lt;br&gt;Composing Symmetries of a Square</td>
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Final exam
Last day for automatic withdrawal:
As the instructor for this course, I reserve the right to adjust this schedule in any way that serves the educational needs of the students enrolled in this course.

Student Learning Outcomes: There will be almost no lecturing in this course. To help you develop your intuitive reasoning and problem-solving skills, we will spend most of our class time working in small groups on problems from the course packet. An important part of learning to solve problems is being willing to struggle with a problem even after you get stuck, and this is one of the first things you will face this term. You may be surprised by how much you can do if you just keep at it! We will usually discuss the problems in a large group after most groups have finished them. Sometimes you will be asked to write up your ideas and solutions, but always you are expected to think about the problems, participate in solving them, and communicate your ideas with others. Communicating your ideas clearly to others is as important as developing them in the first place. Note that this is a math content course, and not a pedagogy course. We hope that taking this course will help you be a better teacher, but more by setting an example rather than teaching you math methods. Students who come out of this course generally feel a lot more comfortable about teaching math, and about being a mathematical authority in the classroom. Hang in there!

After completing this course, the student should be able to:

- communicate clear mathematical claims and justifications orally and in writing
- use concrete, pictorial, and symbolic models to explain and justify the Pythagorean Theorem
- calculate vertex angle measures for regular polygons, and explain and justify a general procedure for doing so
- demonstrate and justify tessellations of the plane using an arbitrary triangle or quadrilateral
- provide and justify the exhaustive classification of regular and semiregular tessellations of the plane, and regular polyhedra
• analyze symmetries of planar and solid figures using pictorial and concrete models, respectively

• explain the relationships between perimeter and area of planar figures, and between surface area and volume of solid figures

• explain and justify common formulae for area and volume of geometric figures, using concrete, pictorial, and symbolic representations

• determine, and describe general procedures for determining, areas and volumes of irregular figures, using concrete, pictorial, and symbolic representations

Requirements: Completed Math 1330

Required Textbooks and Other Course Materials: Purchase the Coursepack at Bird’s Copy Shop (817-459-1688) at 208 East St. You will also need scissors, straightedge, compass, pipe cleaners, protractor, and colored pencils.

Descriptions of major assignments and examinations: The exams will be similar in nature to the problems we work in class, but short enough to be completed in the time given. A sample exam will be distributed before each exam in order to give you a closer feel for it, though you should not expect it to serve as an exact blueprint for the real thing. The dates and times for the midterm and final exam (both in our usual room) are given above. Please mark them on your calendar now so as to avoid conflicts. If a conflict arises, please see me as soon as possible to resolve it. No make-up exams will be given without prior arrangement.

THE WRITTEN WORK will have two components: write-ups (also called problem reports) and reflections. A write-up is a detailed solution to a problem we discussed in class. These write-ups should be readable independently of any worksheet on which they are based, in good English and either legibly handwritten in ink or word-processed. They should always include the following (although you need not use this form): 1. a statement of the problem at hand, 2. any strategies you used to attack the problem, 3. the solution you obtained, with an explanation of how you got it (and how you know it is complete), and 4. a conclusion that says what we can take with us from the problem. Communication of what you understand (even if it’s not a complete understanding) is at least as much the point as finding the solution. The write-ups can be uploaded into Blackboard under Course Materials. I will also sometimes ask you to write a reflection on a rather less concrete issue, like “What does it mean to get stuck?” These will often be completed on Blackboard in discussion form and will be graded more loosely, more on how much thought went into it than on organization and content.

I will let you know at the time I assign written work when it is due, but typically it will be due a week from the time it is assigned. You will have roughly one assignment due per week. Each student is allowed **one late submission per semester**, but all written work must he turned in before the same assignment is handed back to the rest of the class, to receive credit. Late submissions after the first week will be accepted at the discretion of the instructor, with penalties. At the end of the semester, each student will have the opportunity to rewrite one
assignment. If you find you are having difficulty with written assignments, I encourage you to consult me, one or the other 1331 instructors, or your classmates, bringing a draft of the paper to go over. Small groups whose members revise each other's drafts historically tend to do better on them.

Assignments: The exact due dates will be assigned throughout semester.

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<th>Reflection in Discussion format online</th>
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<td>Week 10</td>
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<td>Composing Symmetries of a Square</td>
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<tr>
<td>Week 11</td>
<td>Reflection 10</td>
<td>Three Reflections</td>
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These are your blackboards. Own the classroom.

Attendance: ATTENDANCE AND PARTICIPATION are a significant part of your grade because this course is more an experience than a set of material to be learned. Most of what I hope will happen for you in this course will take place inside the classroom, working in groups and talking with others. Attendance will be taken by means of a daily sign-in sheet. You may miss up to 3 days (excused or not) without penalty; after that your grade is multiplied by the proportion of classes attended. Arriving late (after we have started class) or leaving early counts as half an absence. It also means missing important announcements, often made at the beginning or end of class. Students with special needs, or other situation which affects their attendance for several consecutive classes, should consult with the instructor as soon as possible. It is also in your interest to
participate in the group problem solving sessions since active learning is better than passive learning. Participation includes both small and large group work. Participation in small groups means coming to class prepared (working on a problem outside of class, or bringing requested materials to class), working productively with groupmates, and making sure everyone in your small group follows what you are doing. Large group participation means making some sort of tangible contribution. If you don’t feel comfortable answering questions, ask one of your own questions spur discussion as much as answers. You’ll be doing a favor to classmates wondering the same thing.

**Grading:** Students are expected to keep track of their performance throughout the semester on Blackboard and seek guidance from available sources (including the instructor) if their performance drops below satisfactory levels. Your grade for the course will be determined by two exams (20% each), by attendance and participation (20%), and in large part by written work you will turn in (40%). Assignments will be uploaded on Blackboard.

**Make-up Exams:** Please mark them on your calendar now so as to avoid conflicts. If a conflict arises, please see me as soon as possible to resolve it. No make-up exams will be given without prior arrangement.

**Expectations for Out-of-Class Study:** Beyond the time required to attend each class meeting, students enrolled in this course should expect to spend at least an additional 6 hours per week of their own time in course-related activities, including reading required materials, completing assignments, preparing for exams, etc.

**Grade Grievances:** Any appeal of a grade in this course must follow the procedures and deadlines for grade-related grievances as published in the current undergraduate catalog. [For undergraduate courses, see http://wweb.uta.edu/catalog/content/general/academic_regulations.aspx#10.]

**Drop Policy:** Students may drop or swap (adding and dropping a class concurrently) classes through self-service in MyMav from the beginning of the registration period through the late registration period. After the late registration period, students must see their academic advisor to drop a class or withdraw. Undeclared students must see an advisor in the University Advising Center. Drops can continue through a point two-thirds of the way through the term or session. It is the student's responsibility to officially withdraw if they do not plan to attend after registering. **Students will not be automatically dropped for non-attendance.** Repayment of certain types of financial aid administered through the University may be required as the result of dropping classes or withdrawing. For more information, contact the Office of Financial Aid and Scholarships (http://wweb.uta.edu/ses/fao).

**Academic Integrity:** All students enrolled in this course are expected to adhere to the UT Arlington Honor Code:

_I pledge, on my honor, to uphold UT Arlington’s tradition of academic integrity, a tradition that values hard work and honest effort in the pursuit of academic excellence._

_I promise that I will submit only work that I personally create or contribute to group collaborations, and I will appropriately reference any work from other sources. I will follow the highest standards of integrity and uphold the spirit of the Honor Code._

Instructors may employ the Honor Code as they see fit in their courses, including (but not limited to) having students acknowledge the honor code as part of an examination or requiring students to incorporate the honor code into any work submitted. Per UT System Regents’ Rule 50101, §2.2, suspected violations of university’s standards for academic integrity (including the Honor Code) will
be referred to the Office of Student Conduct. Violators will be disciplined in accordance with University policy, which may result in the student’s suspension or expulsion from the University.

**Americans with Disabilities Act:** The University of Texas at Arlington is on record as being committed to both the spirit and letter of all federal equal opportunity legislation, including the *Americans with Disabilities Act (ADA).* All instructors at UT Arlington are required by law to provide "reasonable accommodations" to students with disabilities, so as not to discriminate on the basis of that disability. Any student requiring an accommodation for this course must provide the instructor with official documentation in the form of a letter certified by the staff in the Office for Students with Disabilities, University Hall 102. Only those students who have officially documented a need for an accommodation will have their request honored. Information regarding diagnostic criteria and policies for obtaining disability-based academic accommodations can be found at [www.uta.edu/disability](http://www.uta.edu/disability) or by calling the Office for Students with Disabilities at (817) 272-3364.

**Academic Integrity:** At UT Arlington, academic dishonesty is completely unacceptable and will not be tolerated in any form, including (but not limited to) “cheating, plagiarism, collusion, the submission for credit of any work or materials that are attributable in whole or in part to another person, taking an examination for another person, any act designed to give unfair advantage to a student or the attempt to commit such acts” (UT System Regents’ Rule 50101, §2.2). Suspected violations of academic integrity standards will be referred to the Office of Student Conduct. Violators will be disciplined in accordance with University policy, which may result in the student’s suspension or expulsion from the University.

**Student Support Services:** UT Arlington provides a variety of resources and programs designed to help students develop academic skills, deal with personal situations, and better understand concepts and information related to their courses. Resources include tutoring, major-based learning centers, developmental education, advising and mentoring, personal counseling, and federally funded programs. For individualized referrals, students may visit the reception desk at University College (Ransom Hall), call the Maverick Resource Hotline at 817-272-6107, send a message to resources@uta.edu, or view the information at [www.uta.edu/resources](http://www.uta.edu/resources).

**Electronic Communication:** UT Arlington has adopted MavMail as its official means to communicate with students about important deadlines and events, as well as to transact university-related business regarding financial aid, tuition, grades, graduation, etc. All students are assigned a MavMail account and are responsible for checking the inbox regularly. There is no additional charge to students for using this account, which remains active even after graduation. Information about activating and using MavMail is available at [http://www.uta.edu/oit/cs/email/mavmail.php](http://www.uta.edu/oit/cs/email/mavmail.php).

**Student Feedback Survey:** At the end of each term, students enrolled in classes categorized as lecture, seminar, or laboratory shall be directed to complete a Student Feedback Survey (SFS). Instructions on how to access the SFS for this course will be sent directly to each student through MavMail approximately 10 days before the end of the term. Each student’s feedback enters the SFS database anonymously and is aggregated with that of other students enrolled in the course. UT Arlington’s effort to solicit, gather, tabulate, and publish student feedback is required by state law; students are strongly urged to participate. For more information, visit [http://www.uta.edu/sfs](http://www.uta.edu/sfs).

**Final Review Week:** A period of five class days prior to the first day of final examinations in the long sessions shall be designated as Final Review Week. The purpose of this week is to allow students sufficient time to prepare for final examinations. During this week, there shall be no scheduled activities such as required field trips or performances; and no instructor shall assign any
themes, research problems or exercises of similar scope that have a completion date during or following this week unless specified in the class syllabus. During Final Review Week, an instructor shall not give any examinations constituting 10% or more of the final grade, except makeup tests and laboratory examinations. In addition, no instructor shall give any portion of the final examination during Final Review Week. During this week, classes are held as scheduled. In addition, instructors are not required to limit content to topics that have been previously covered; they may introduce new concepts as appropriate.

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**Signature Assignment- Circle Construction**

Investigate the following questions with your group. Analyze how to answer the questions visually but also include a verbal justification on “why” the answers are correct. Use definitions and theorems to prove that the supporting diagrams are correct.

1. Draw any three noncollinear points on a piece of paper. Can you construct a circle containing them on its circumference?
2. Can you construct a different one through the same three points from number one? How many different circles are there through those three points?
3. Can you construct a circle through three collinear points?

After these questions are analyzed, you need to submit a problem report that presents your analysis of the three questions along with your arguments supporting your conclusions. You will need to include the diagrams constructed in order to answer the questions. After visually supporting your answers, you will need to develop verbal arguments using definitions and theorems in order to verify each of your answers.

**Use this checklist as a guide for your problem report:**

Does the paper:

1. clearly state the problems to be solved?
2. state the answers in complete sentences that stand on their own?
3. define all variables, terminology, and notation used?
4. explain how each theorem is derived?
5. clearly label any diagrams?
6. give a precise and well-organized explanation of the definitions and theorems supporting each of the answers?
7. contain correct mathematics?

**Overall, the problem report needs to effectively communicate:**

- the given questions with clarity and their solutions.
- the role of the perpendicular bisectors.
- a labeled diagram with construction marks for both question 1 and 3.
- how the center of the circle was found.
- to the reader that your circle’s center was actually a circle passing through the three original points both visually and verbally. (The argument should support the position of any three noncollinear points.)
- the justification of how many circles can be constructed through three noncollinear points.
- the justification of why or why not a circle can be constructed through three collinear points.
Rubric used out of a 10 point scale:
Clarity of instructions (1 point)
Describe role of perpendicular bisectors (1 point)
Specify how to find center (1 point)
Justification: convince reader it works (3 points) [make the connection for all three radii not just two by using perpendicular bisector theorems]
Diagrams (2 points): for both collinear and noncollinear points, labels, and actually includes circle
Are there any other circles through these three points? Why or why not? (1 point)
Can you draw a circle through three noncollinear points? Why or why not? (1 point)