Chapter 18
Electric Currents
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Volta discovered that electricity could be created if dissimilar metals were connected by a conductive solution called an electrolyte.

This is a simple electric cell.
A battery transforms chemical energy into electrical energy.

Chemical reactions within the cell create a potential difference between the terminals by slowly dissolving them. This potential difference can be maintained even if a current is kept flowing, until one or the other terminal is completely dissolved.
Several cells connected together make a battery, although now we refer to a single cell as a battery as well.
18-2 Electric Current

Electric current is the rate of flow of charge through a conductor:

\[ I = \frac{\Delta Q}{\Delta t} \quad (18-1) \]

Unit of electric current: the ampere, A.

\[ 1 \text{ A} = 1 \text{ C/s} \]
18-2 Electric Current

A complete circuit is one where current can flow all the way around. Note that the schematic drawing doesn’t look much like the physical circuit!
In order for current to flow, there must be a path from one battery terminal, through the circuit, and back to the other battery terminal. Only one of these circuits will work:
By convention, current is defined as flowing from + to –. Electrons actually flow in the opposite direction, but not all currents consist of electrons.
18-3 Ohm’s Law: Resistance and Resistors

Experimentally, it is found that the current in a wire is proportional to the potential difference between its ends:

\[ I \propto V \]
18-3 Ohm’s Law: Resistance and Resistors

The ratio of voltage to current is called the resistance:

\[ V = IR. \]

(18-2)
Standard resistors are manufactured for use in electric circuits; they are color-coded to indicate their value and precision.
# 18-3 Ohm’s Law: Resistance and Resistors

<table>
<thead>
<tr>
<th>Resistor Color Code</th>
</tr>
</thead>
<tbody>
<tr>
<td>Color</td>
</tr>
<tr>
<td>Black</td>
</tr>
<tr>
<td>Brown</td>
</tr>
<tr>
<td>Red</td>
</tr>
<tr>
<td>Orange</td>
</tr>
<tr>
<td>Yellow</td>
</tr>
<tr>
<td>Green</td>
</tr>
<tr>
<td>Blue</td>
</tr>
<tr>
<td>Violet</td>
</tr>
<tr>
<td>Gray</td>
</tr>
<tr>
<td>White</td>
</tr>
<tr>
<td>Gold</td>
</tr>
<tr>
<td>Silver</td>
</tr>
<tr>
<td>No color</td>
</tr>
</tbody>
</table>
Some clarifications:

- Batteries maintain a (nearly) constant potential difference; the current varies.
- Resistance is a property of a material or device.
- Current is not a vector but it does have a direction.
- Current and charge do not get used up. Whatever charge goes in one end of a circuit comes out the other end.
18-4 Resistivity

The resistance of a wire is directly proportional to its length and inversely proportional to its cross-sectional area:

\[ R = \rho \frac{\ell}{A} \quad (18-3) \]

The constant \( \rho \), the resistivity, is characteristic of the material.
18-4 Resistivity

<table>
<thead>
<tr>
<th>Material</th>
<th>Resistivity, $\rho$ ((\Omega \cdot m))</th>
<th>Temperature Coefficient, $\alpha$ ((^{\circ}\text{C})^{-1})</th>
</tr>
</thead>
<tbody>
<tr>
<td>Conductors</td>
<td></td>
<td></td>
</tr>
<tr>
<td>Silver</td>
<td>$1.59 \times 10^{-8}$</td>
<td>0.0061</td>
</tr>
<tr>
<td>Copper</td>
<td>$1.68 \times 10^{-8}$</td>
<td>0.0068</td>
</tr>
<tr>
<td>Gold</td>
<td>$2.44 \times 10^{-8}$</td>
<td>0.0034</td>
</tr>
<tr>
<td>Aluminum</td>
<td>$2.65 \times 10^{-8}$</td>
<td>0.00429</td>
</tr>
<tr>
<td>Tungsten</td>
<td>$5.6 \times 10^{-8}$</td>
<td>0.0045</td>
</tr>
<tr>
<td>Iron</td>
<td>$9.71 \times 10^{-8}$</td>
<td>0.00651</td>
</tr>
<tr>
<td>Platinum</td>
<td>$10.6 \times 10^{-8}$</td>
<td>0.003927</td>
</tr>
<tr>
<td>Mercury</td>
<td>$98 \times 10^{-8}$</td>
<td>0.0009</td>
</tr>
<tr>
<td>Nichrome (Ni, Fe, Cr alloy)</td>
<td>$100 \times 10^{-8}$</td>
<td>0.0004</td>
</tr>
<tr>
<td>Semiconductors(^\ddagger)</td>
<td></td>
<td></td>
</tr>
<tr>
<td>Carbon (graphite)</td>
<td>$(3-60) \times 10^{-5}$</td>
<td>-0.0005</td>
</tr>
<tr>
<td>Germanium</td>
<td>$(1-500) \times 10^{-3}$</td>
<td>-0.05</td>
</tr>
<tr>
<td>Silicon</td>
<td>$0.1-60$</td>
<td>-0.07</td>
</tr>
<tr>
<td>Insulators</td>
<td></td>
<td></td>
</tr>
<tr>
<td>Glass</td>
<td>$10^9-10^{12}$</td>
<td></td>
</tr>
<tr>
<td>Hard rubber</td>
<td>$10^{13}-10^{15}$</td>
<td></td>
</tr>
</tbody>
</table>

\(^\ddagger\) Values depend strongly on the presence of even slight amounts of impurities.
18-4 Resistivity

A wire with a circular cross section and a resistance $R$ is lengthened to 6.04 times its original length by pulling it through a small hole. The total volume of the wire is unchanged. Find the resistance of the wire after it is stretched.
For any given material, the resistivity increases with temperature:

$$\rho_T = \rho_0 [1 + \alpha(T - T_0)]$$  (18-4)

Semiconductors are complex materials, and may have resistivities that decrease with temperature.
18-5 Electric Power

Power, as in kinematics, is the energy transformed by a device per unit time:

\[ P = \frac{\text{energy transformed}}{\text{time}} = \frac{QV}{t}. \]

\[ P = IV. \]  

(18-5)
18-5 Electric Power

The unit of power is the watt, $W$.

For ohmic devices, we can make the substitutions:

\[ P = IV = I(IR) = I^2R \quad (18-6a) \]

\[ P = IV = \left( \frac{V}{R} \right)V = \frac{V^2}{R} \quad (18-6b) \]
18-5 Electric Power

What you pay for on your electric bill is not power, but energy—the power consumption multiplied by the time. We have been measuring energy in joules, but the electric company measures it in kilowatt-hours, kWh.

One kWh = (1000 W)(3600 s) = 3.60 \times 10^6 J
Examples

• Practice example 18-10
• Page 512.
• An electric air conditioning unit draws 15 amps of direct current from a 102 V direct voltage source, and is used 24 hours a day during 23.6 days in July. How much will the electricity cost for the month if the local electrical rate is 8.8 cents/kW · hr?
Current from a battery flows steadily in one direction (direct current, DC). Current from a power plant varies sinusoidally (alternating current, AC).
18-7 Alternating Current

The voltage varies sinusoidally with time:

\[ V = V_0 \sin 2\pi ft = V_0 \sin \omega t \quad (18-7a) \]

V oscillates between \( +V_0 \) and \( -V_0 \) (\( V_0 \) peak voltage)

Frequency: oscillations made per second

….as does the current:

\[ I = \frac{V}{R} = \frac{V_0}{R} \sin \omega t = I_0 \sin \omega t. \quad (18-7b) \]

Peak current \( I_0 = \frac{V_0}{R} \)

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Multiplying the current and the voltage gives the power:

\[ P = I^2R = I_0^2 R \sin^2 \omega t. \]
18-7 Alternating Current

Usually we are interested in the average power:

\[ \bar{P} = \frac{1}{2} I_0^2 R \]

\[ \bar{P} = \frac{1}{2} \frac{V_0^2}{R} \]

NOTES!
18-7 Alternating Current

The current and voltage both have average values of zero, so we square them, take the average, then take the square root, yielding the root mean square (rms) value.

\[ I_{\text{rms}} = \sqrt{I^2} = \frac{I_0}{\sqrt{2}} = 0.707 I_0 \]  \hspace{1cm} (18-8a)

\[ V_{\text{rms}} = \sqrt{V^2} = \frac{V_0}{\sqrt{2}} = 0.707 V_0. \]  \hspace{1cm} (18-8b)
The output of a generator is given by $v(t) = a \sin(\omega t)$, where $a = 186 \text{ V}$.

Find the rms current in the circuit when this generator is connected to a 147 $\Omega$ resistor.
In general, resistivity decreases as temperature decreases. Some materials, however, have resistivity that falls abruptly to zero at a very low temperature, called the critical temperature, $T_C$. 

![Graph showing resistivity $\rho$ vs temperature $T$ with a sharp drop at $T_C$.]

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18-9 Superconductivity

Experiments have shown that currents, once started, can flow through these materials for years without decreasing even without a potential difference.

Critical temperatures are low; for many years no material was found to be superconducting above 23 K.

More recently, novel materials have been found to be superconducting below 90 K, critical temperatures as high as 160K have been reported.
18-10 Electrical Conduction in the Human Nervous System

The human nervous system depends on the flow of electric charge.

The basic elements of the nervous system are cells called neurons.

Neurons have a main cell body, small attachments called dendrites, and a long tail called the axon.
18-10 Electrical Conduction in the Human Nervous System

Signals are received by the dendrites, propagated along the axon, and transmitted through a connection called a synapse.
18-10 Electrical Conduction in the Human Nervous System

This process depends on there being a dipole layer of charge on the cell membrane, and different concentrations of ions inside and outside the cell.
This applies to most cells in the body. Neurons can respond to a stimulus and conduct an electrical signal. This signal is in the form of an action potential.
The action potential propagates along the axon membrane.
Summary of Chapter 18

- A battery is a source of constant potential difference.
- Electric current is the rate of flow of electric charge.
- Conventional current is in the direction that positive charge would flow.
- Resistance is the ratio of voltage to current:  \( V = IR \).
Summary of Chapter 18

- Ohmic materials have constant resistance, independent of voltage.
- Resistance is determined by shape and material: $R = \rho \frac{\ell}{A}$
- $\rho$ is the resistivity.
- Power in an electric circuit: $P = IV$. 
Summary of Chapter 18

• Direct current is constant

• Alternating current varies sinusoidally

\[ I = \frac{V}{R} = \frac{V_0}{R} \sin \omega t = I_0 \sin \omega t \]

• The average (rms) current and voltage:

\[ I_{\text{rms}} = \sqrt{I^2} = \frac{I_0}{\sqrt{2}} = 0.707I_0 \]

\[ V_{\text{rms}} = \sqrt{V^2} = \frac{V_0}{\sqrt{2}} = 0.707V_0 \]

• The average (rms) current and voltage:

\[ I = \frac{\Delta Q}{\Delta t} = neAv_d \]